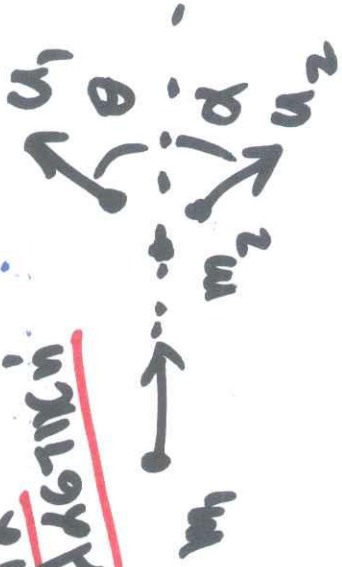


31/12/21

~~πλδγβ~~
~~ελδγβ~~



①

ΦΥΣΙΚΗ

$$\vec{P}_1 = \vec{P}'_1 + \vec{P}'_2 \Rightarrow \vec{P}'_1 = (\vec{P}_1 - \vec{P}'_2)$$

$$P_1^2 / 2m_1 = P_1'^2 / 2m_1 + P_2'^2 / 2m_2$$

$$\left. \begin{aligned} P_1^2 &= \vec{P}_1^2 + \vec{P}_2^2 - 2\vec{P}_1 \cdot \vec{P}_2 \\ P_1^2 &= \vec{P}_1^2 - \vec{P}_2^2 + 2\vec{P}_1 \cdot \vec{P}_2 \end{aligned} \right\}$$

$$P_2^2 \left(1 + \frac{m_1}{m_2}\right) = 2\vec{P}_1 \cdot \vec{P}_2' = 2P_1 P_2' \cos \alpha$$

$$\cancel{m_2}^2 \cancel{u_2}^2 \left(\frac{m_1 + m_2}{m_2}\right) = 2m_1 u_1 \cancel{u_2}^2 \cos \alpha$$

$$u_2 = \frac{2m_1}{m_1 + m_2} u_1 \cos \alpha$$

2

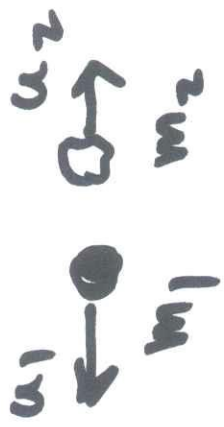
ΕΡΧΕΤΑΙ ΔΥΟ ΘΡΑΥΣΜΑΤΩΝ 1 → 2

$$Q = \frac{1}{2} m_1 u_1^2 + \frac{1}{2} m_2 u_2^2 = 0$$

$$= \frac{1}{2} \mu u^2$$

$$m_1 u_1 + m_2 u_2 = 0$$

ΠΡΗΝ



ΜΕΤΑ

$$Q = \frac{1}{2} m_1 u_1^2 + \frac{1}{2} m_2 u_2^2$$

$$u_2 = -u_1 \frac{m_1}{m_2}$$

$$u_1 - u_2 = \sqrt{\frac{2Q}{\mu}}$$

$$u_1 \left(1 + \frac{m_1}{m_2}\right) = \sqrt{\frac{2Q}{\mu}}$$

$$u_1 = \frac{\sqrt{\frac{2Q}{\mu}}}{1 + m_1/m_2}$$

$$u_2 = -\frac{\sqrt{\frac{2Q}{\mu}}}{1 + m_2/m_1}$$

ΣΥΓΚΕΚΡΙΜΕΝΕΣ ΤΑΧΥΤΗΤΕΣ

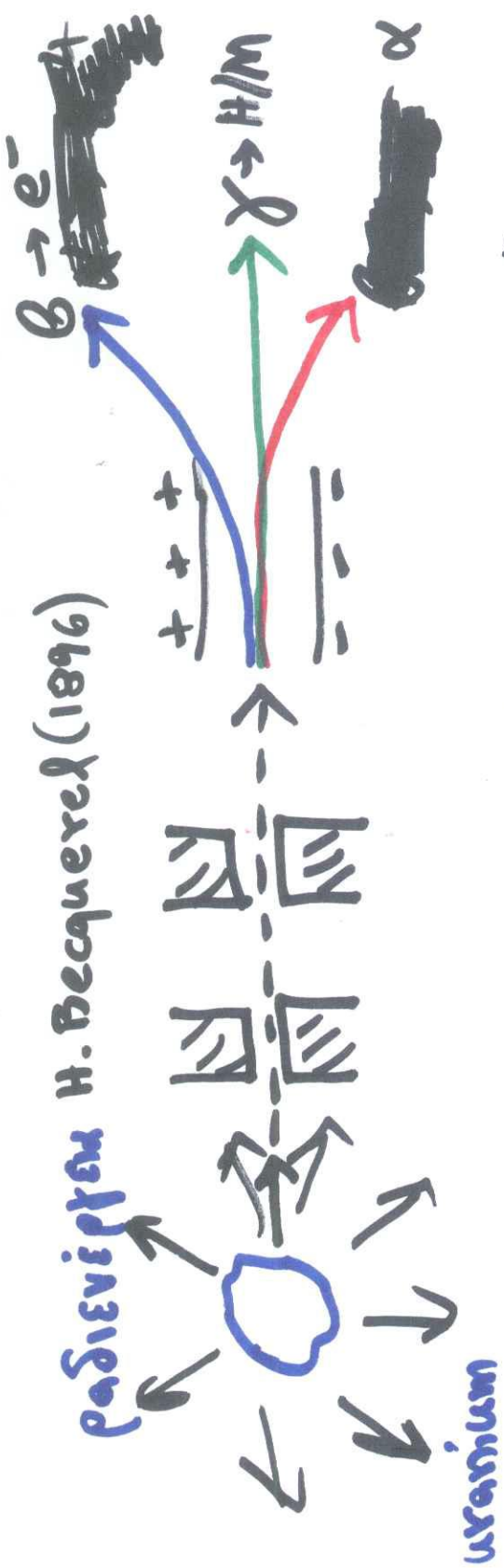
$$P_1 = m_1 u_1 = \mu \sqrt{\frac{2Q}{\mu}}$$

$$= \sqrt{2Q\mu}$$

$$P_2 = \dots = \sqrt{2Q\mu}$$

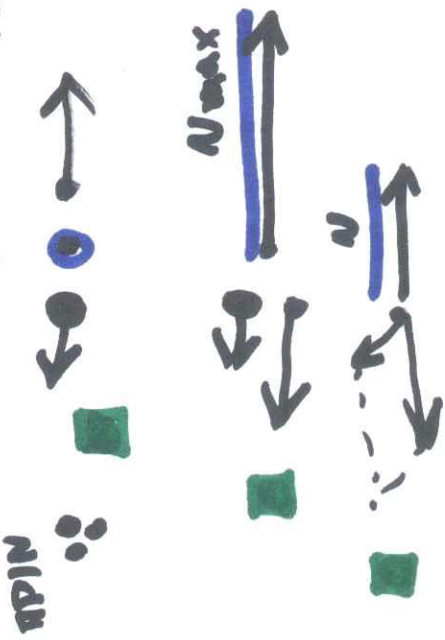
ραδιενέργεια H. Becquerel (1896)

3



1 → 3 οχι συγκεκριμένες ταχύτητες

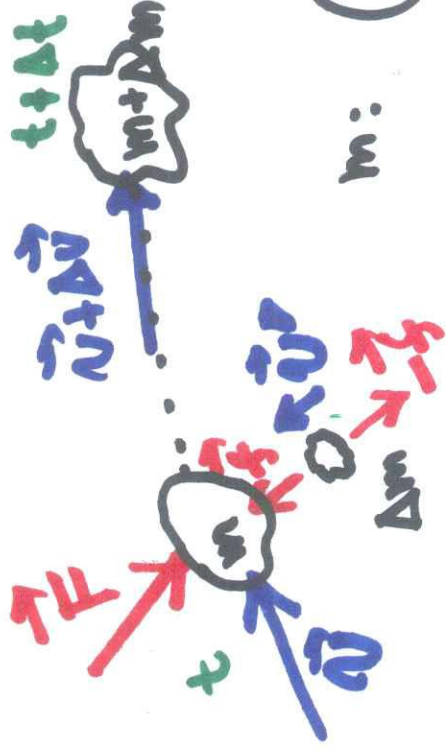
also μετά



Η απώθηση της ύπαρξης του νετρίνου και η μετεπειτα ανακάλυψή του

αποκατέστησε την διατήρηση της ορμής και της ενέργειας στην β-διάσπαση

W. Pauli (1930)
 Pauli 1 → 3
 νετρίνο (1956)



④

Approx imo Oppis

$$\Delta\vec{p} = \vec{F} \Delta t$$

$$m: (m(\vec{v} + \Delta\vec{v})) - m\vec{v} = \vec{F} \Delta t + \cancel{\vec{F} \Delta t}$$

$$\Delta m: \Delta m(\vec{v} + \Delta\vec{v}) - \Delta m\vec{v} = -\vec{F} \Delta t$$

~~$$m\Delta\vec{v} + \Delta m\vec{v} = \Delta(m\vec{v})$$~~

~~Am~~

$$m\Delta\vec{v} + \Delta m\vec{v} + \Delta m\Delta\vec{v} - \Delta m\vec{v} = \vec{F} \Delta t$$

$$m \frac{\Delta\vec{v}}{\Delta t} + \frac{\Delta m(\vec{v} - \vec{v}')}{\Delta t} + \cancel{\frac{\Delta m\Delta\vec{v}}{\Delta t}} = \vec{F}$$

lim $m \rightarrow 0$
 $\Delta t \rightarrow 0$

$$m \frac{d\vec{v}}{dt} = \vec{F} + \frac{dm}{dt}(\vec{v}' - \vec{v})$$

5

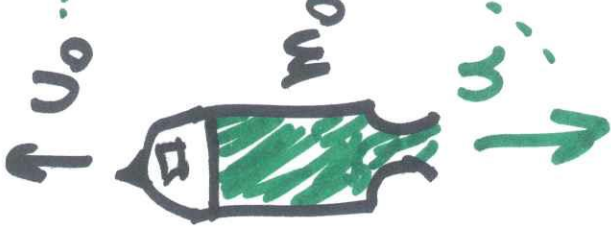
πρώην \hat{u}
αερίων δύναμη
(thrust) $\vec{F}_T = \vec{u} \frac{dm}{dt}$

$$\vec{F}_T = \vec{u} \frac{dm}{dt}$$

σταδ.

ΠΥΡΑΥΛΟΣ = (ΕΞΟΠΛΙΣΜΟΣ + ΠΡΟΣΩΠΙΚΟ + ΟΦΕΝ. ΦΟΡΤΙΟ)

... \hat{u} ... $\frac{dm}{dt}$... + (ΚΑΥΣΙΜΑ) ΜΕΤΑΒΛ.



$$m \frac{dv}{dt} = - \frac{dm}{dt} u$$

$$u = 4,5 \text{ km/s}$$

Δu

$$\int_{u_0}^u \frac{dv}{u} = \int_{m_0}^m \frac{dm}{m} \Rightarrow \frac{v-u_0}{u} = - \ln\left(\frac{m}{m_0}\right)$$

$$e^{-\Delta v/u} = \frac{m}{m_0}$$

$$m = m_0 e^{-\Delta v/u}$$

$$v = u_0 + u \ln\left(\frac{m_0}{m}\right)$$

$\frac{dm}{dt}$